

For the following 6 problems, solve one by each method - elimination, substitution, Cramer's Rule, and the inverse of the coefficient matrix. The remaining problems may be solved using any method.

1. $x + 7y = -38$
 $7x + 7y = -14$

2. $x + 6y = -2$
 $-3x + 7y = 6$

3. $x - 2y = -2$
 $5x - y = -10$

4. $6x + 4y = -4$
 $3x + y = -7$

5. $-3x - 5y = 19$
 $-6x - 10y = 17$

6. $x + 4y = -25$
 $x - y = -10$

Solve.

7. Tickets for the school play cost \$6 for students and \$9 for adults. On opening night, all 360 seats were filled and the box office revenues were \$2610. How many student and how many adult tickets were sold?

8. In a chemistry class, 3 liters of a 4% silver iodide solution must be mixed with a 10% solution to get a 6% solution. How many liters of the 10% solution are needed?

9. Find the determinant of the matrix: $\begin{bmatrix} -1 & 2 \\ 2 & 3 \end{bmatrix}$

10. Let $B = \begin{bmatrix} -1 & 4 & 7 & -3 \end{bmatrix}$ Find $-4B$

11. Let $A = \begin{bmatrix} 1 & 3 \\ 2 & 4 \end{bmatrix}$ and $B = \begin{bmatrix} 0 & 4 \\ -1 & 6 \end{bmatrix}$ Find $2A + B$

12. Use the inverse of the coefficient matrix to solve this system of equations.

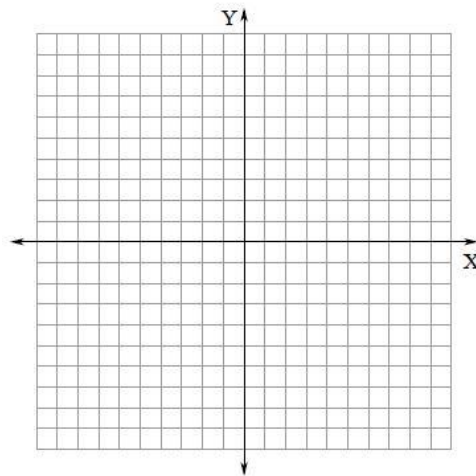
$$\begin{aligned} 5x + 22y &= 13 \\ 2x + 9y &= 6 \end{aligned}$$

13. Find the product, if possible. $\begin{bmatrix} -4 & -4 & 9 \\ -5 & 6 & -6 \end{bmatrix} \cdot \begin{bmatrix} -1 \\ -8 \\ 4 \end{bmatrix}$

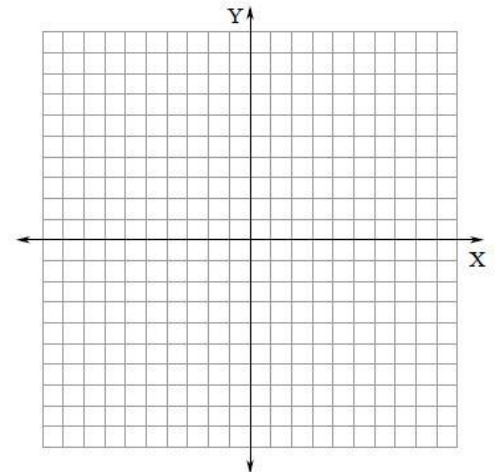
14. Graph the system of inequalities.

$$2x + y \leq 4$$

$$y - 1 \leq 0$$



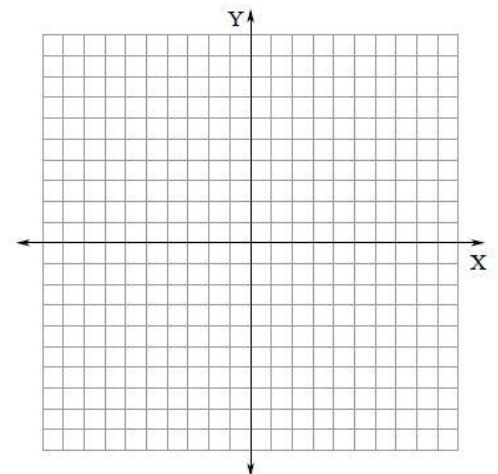
15. A 4-H member raises only geese and pigs. She wants to raise no more than 16 animals, including no more than 10 geese. She spends \$5 to raise a goose and \$15 to raise a pig, and she has \$180 available for this project. Each goose produces \$6 in profit, and each pig produces \$20 in profit. How many of each animal should she raise to maximize her profit? What is her maximum profit?



16. Graph the system of inequalities and find the coordinates of the vertices.

$$x + 2y \leq 2$$

$$x + y \geq 0$$



17. Find A^{-1} if it exists. $A = \begin{bmatrix} -2 & -3 \\ -3 & 9 \end{bmatrix}$

18. Find A^{-1} if it exists. $A = \begin{bmatrix} 2 & -5 \\ 1 & 4 \end{bmatrix}$