

$$z = (\bar{x} - \mu) / \sigma_{\bar{x}} = (241 - 254) / 3.2 = -2.50$$

Step 5: For  $\alpha = .01$ , do not reject  $H_0$  since  $-2.50 > -2.58$ .

For  $\alpha = .02$ , reject  $H_0$  since  $-2.50 < -2.33$ .

For both parts a and b, conclude the mean time spent walking per month by such people does not differ from 254 minutes at  $\alpha = .01$ , but does differ from 254 minutes at  $\alpha = .02$ .

9.39

a. Step 1:  $H_0: \mu = 10$  minutes,  $H_1: \mu \neq 10$  minutes

Step 2: Since  $n > 30$ , use the normal distribution.

Step 3:  $\sigma_{\bar{x}} = \sigma / \sqrt{n} = 3.80 / \sqrt{100} = .38$  minute

$$z = (\bar{x} - \mu) / \sigma_{\bar{x}} = (9.20 - 10) / .38 = -2.11$$

From the normal distribution table, area to the left of  $z = -2.11$  is .0174.

$$p\text{-value} = 2(.0174) = .0348$$

Step 4: For  $\alpha = .02$ , do not reject  $H_0$  since  $.0348 > .02$ .

For  $\alpha = .05$ , reject  $H_0$  since  $.0348 < .05$ .

b. Step 1:  $H_0: \mu = 10$  minutes,  $H_1: \mu \neq 10$  minutes

Step 2: Since  $n > 30$ , use the normal distribution.

Step 3: For  $\alpha = .02$ , the critical values of  $z$  are  $-2.33$  and  $2.33$ .

For  $\alpha = .05$ , the critical values of  $z$  are  $-1.96$  and  $1.96$ .

Step 4:  $\sigma_{\bar{x}} = \sigma / \sqrt{n} = 3.80 / \sqrt{100} = .38$  minute

$$z = (\bar{x} - \mu) / \sigma_{\bar{x}} = (9.20 - 10) / .38 = -2.11$$

Step 5: For  $\alpha = .02$ , do not reject  $H_0$  since  $-2.11 > -2.33$ .

For  $\alpha = .05$ , reject  $H_0$  since  $-2.11 < -1.96$ .

For both parts a and b, conclude the mean duration of long-distance calls made by residential customers does not differ from 10 minutes at  $\alpha = .02$ , but does differ from 10 minutes at  $\alpha = .05$ .

9.40

a. Step 1:  $H_0: \mu = 36$  inches,  $H_1: \mu \neq 36$  inches

Step 2: Since the population is normally distributed, use the normal distribution.

Step 3:  $\sigma_{\bar{x}} = \sigma / \sqrt{n} = .035 / \sqrt{20} = .00782624$  inch

$$z = (\bar{x} - \mu) / \sigma_{\bar{x}} = (36.015 - 36) / .00782624 = 1.92$$

From the normal distribution table, area to the right of  $z = 1.92$  is  $1 - .9726 = .0274$ .

$$p\text{-value} = 2(.0274) = .0548$$

Step 4: For  $\alpha = .02$ , do not reject  $H_0$  since  $.0548 > .02$ .

For  $\alpha = .10$ , reject  $H_0$  since  $.0548 < .10$ .

b. Step 1:  $H_0: \mu = 36$  inches,  $H_1: \mu \neq 36$  inches

Step 2: Since the population is normally distributed, use the normal distribution.

Step 3: For  $\alpha = .02$ , the critical values of  $z$  are  $-2.33$  and  $2.33$ .

For  $\alpha = .10$ , the critical values of  $z$  are  $-1.65$  and  $1.65$ .

$$\begin{aligned}\text{Step 4: } \sigma_{\bar{x}} &= \sigma/\sqrt{n} = .035/\sqrt{20} = .00782624 \text{ inch} \\ z &= (\bar{x} - \mu) / \sigma_{\bar{x}} = (36.015 - 36) / .00782624 = 1.92\end{aligned}$$

Step 5: For  $\alpha = .02$ , do not reject  $H_0$  since  $1.92 < 2.33$ .

For  $\alpha = .10$ , reject  $H_0$  since  $1.92 > 1.65$ .

For both parts a and b, the inspector will not stop this machine at  $\alpha = .02$ , but will stop this machine and adjust it at  $\alpha = .10$ .

- 9.41 a. Step 1:  $H_0: \mu = 32$  ounces,  $H_1: \mu \neq 32$  ounces  
 Step 2: Since the population is normally distributed, use the normal distribution.  
 Step 3:  $\sigma_{\bar{x}} = \sigma/\sqrt{n} = .15/\sqrt{25} = .03$  ounce  
 $z = (\bar{x} - \mu) / \sigma_{\bar{x}} = (31.93 - 32) / .03 = -2.33$   
 From the normal distribution table, area to the left of  $z = -2.33$  is  $.01$ .  
 $p\text{-value} = 2(.01) = .02$   
 Step 4: For  $\alpha = .01$ , do not reject  $H_0$  since  $.02 > .01$ .  
 For  $\alpha = .05$ , reject  $H_0$  since  $.02 < .05$ .
- b. Step 1:  $H_0: \mu = 32$  ounces,  $H_1: \mu \neq 32$  ounces  
 Step 2: Since the population is normally distributed, use the normal distribution.  
 Step 3: For  $\alpha = .01$ , the critical values of  $z$  are  $-2.58$  and  $2.58$ .  
 For  $\alpha = .05$ , the critical values of  $z$  are  $-1.96$  and  $1.96$ .  
 Step 4:  $\sigma_{\bar{x}} = \sigma/\sqrt{n} = .15/\sqrt{25} = .03$  ounce  
 $z = (\bar{x} - \mu) / \sigma_{\bar{x}} = (31.93 - 32) / .03 = -2.33$   
 Step 5: For  $\alpha = .01$ , do not reject  $H_0$  since  $-2.33 > -2.58$ .  
 For  $\alpha = .05$ , reject  $H_0$  since  $-2.33 < -1.96$ .

For both parts a and b, the inspector will not stop this machine at  $\alpha = .01$ , but will stop this machine and adjust it at  $\alpha = .05$ .

- 9.42 a. Step 1:  $H_0: \mu = 11$  hours,  $H_1: \mu < 11$  hours  
 Step 2: Since  $n > 30$ , use the normal distribution.  
 Step 3: For  $\alpha = .01$ , the critical value of  $z$  is  $-2.33$ .  
 Step 4:  $\sigma_{\bar{x}} = \sigma/\sqrt{n} = 2.2/\sqrt{100} = .22$  hour  
 $z = (\bar{x} - \mu) / \sigma_{\bar{x}} = (9 - 11) / .22 = -9.09$   
 Step 5: Reject  $H_0$  since  $-9.09 < -2.33$ .  
 Conclude that adult males spend less than 11 hours watching sports on television.
- b. If  $\alpha = 0$ , there can be no rejection region, and we cannot reject  $H_0$ . Therefore, the decision would be "do not reject  $H_0$ ."

- 9.43 a. Step 1:  $H_0: \mu \geq \$35,000, H_1: \mu < \$35,000$   
 Step 2: Since  $n > 30$ , use the normal distribution.  
 Step 3: For  $\alpha = .01$ , the critical value of  $z$  is  $-2.33$ .  
 Step 4:  $\sigma_{\bar{x}} = \sigma/\sqrt{n} = 5400/\sqrt{150} = \$440.90815370$   
 $z = (\bar{x} - \mu) / \sigma_{\bar{x}} = (33,400 - 35,000) / \$440.90815370 = -3.63$   
 Step 5: Reject  $H_0$  since  $-3.63 < -2.33$ .  
 Conclude that the company should not open a restaurant in this area.
- b. If  $\alpha = 0$ , there can be no rejection region, and we cannot reject  $H_0$ . Therefore, the decision would be "do not reject  $H_0$ ."

- 9.44 a. The first two steps and the calculation of the observed value of the test statistic are the same for both the  $p$ -value approach and critical value approach.

Step 1:  $H_0: \mu \geq 30$  hours,  $H_1: \mu < 30$  hours

Step 2: Since the population is normally distributed, use the normal distribution.

$$\sigma_{\bar{x}} = \sigma/\sqrt{n} = 7/\sqrt{25} = 1.4 \text{ hours}$$

$$z = (\bar{x} - \mu) / \sigma_{\bar{x}} = (27 - 30) / 1.4 = -2.14$$

$p$ -value approach

Step 3: From above,  $z = -2.14$ .

From the normal distribution table, area to the left of  $z = -2.14$  is .0162.

$$p\text{-value} = .0162$$

Step 4: Reject  $H_0$  since  $.0162 < .025$ .

critical value approach

Step 3: For  $\alpha = .025$ , the critical value of  $z$  is  $-1.96$ .

Step 4: From above,  $z = -2.14$ .

Step 5: Reject  $H_0$  since  $-2.14 < -1.96$ .

Conclude that the time per month on such reading by all adults in this city is less than 30 minutes.

- b. For  $\alpha = .01$ , do not reject  $H_0$  using  $p$ -value approach since  $.0162 > .01$ . The critical value of  $z = -1.96$ ; do not reject  $H_0$  since  $-2.14 > -2.33$ .

The decisions in parts a and b are different. The results of this sample are not very conclusive, since lowering the significance level from .025 to .01 reverses the decision.

- 9.45 a. The first two steps and the calculation of the observed value of the test statistic are the same for both the  $p$ -value approach and critical value approach.

Step 1:  $H_0: \mu \geq 8$  hours,  $H_1: \mu < 8$  hours

Step 2: Since the population is normally distributed, use the normal distribution.

$$\sigma_{\bar{x}} = \sigma/\sqrt{n} = 2.1/\sqrt{20} = .46957428 \text{ hour}$$